

# Complementary Classifier Induced Partial Label Learning

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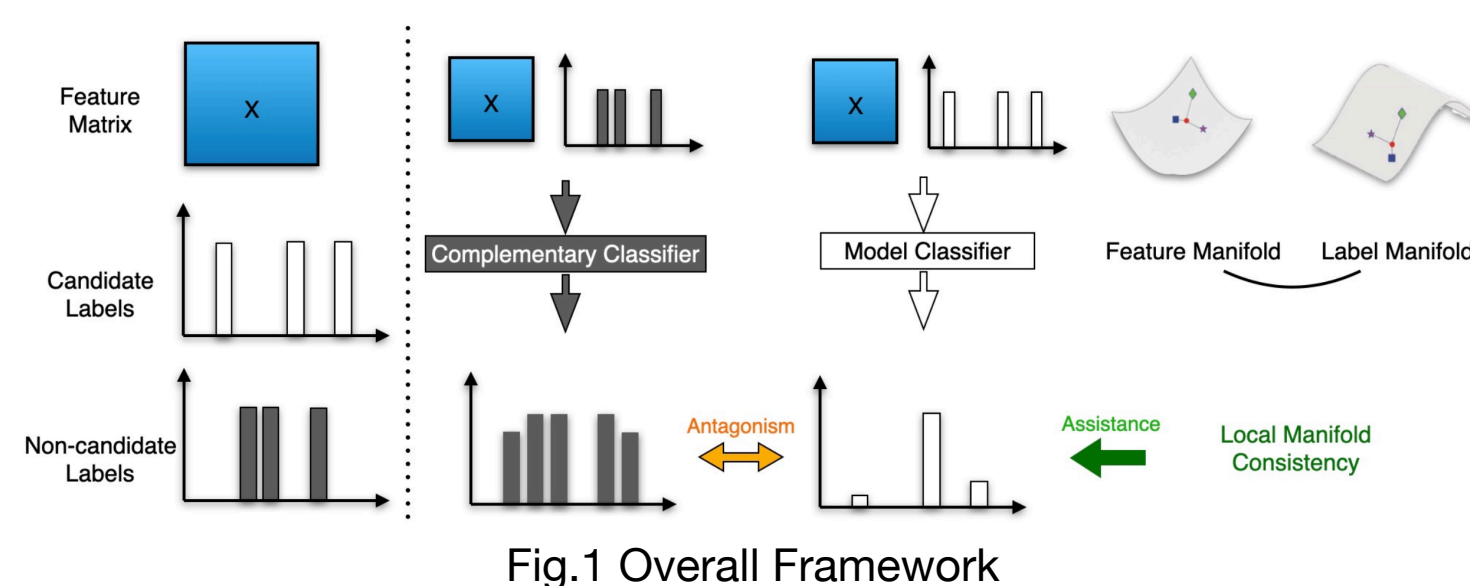


## INTRODUCTION

- **Insight:**
  - There are three kinds of priors that are useful for partial label learning, the correlations among instances, the mapping from instances to the candidate labels and non-candidate labels, i.e., complementary labels.
  - The majority of the existing works overlook the valuable information in complementary labels. To fully take advantage of above mentioned priors, a novel PLL method named PL-CL is proposed.
- **PL-CL:**
  - Construct an ordinary classifier and a complementary classifier.
  - Design an adversarial term to link the outputs of the two classifiers.
  - Construct an adaptive local topological graph shared by both the feature space and the label space
- **Contributions:**
  - We first propose a complementary classifier, which has never been studied in the partial label literature.
  - We propose an adversarial term to link the ordinary classifier and the complementary classifier.
  - We conducted extensive experiments to show the effectiveness of PL-CL.

## METHOD

- **PL-CL:** Fig.1 shows the overall framework of PL-CL.



- **PL-CL:** The loss function of PL-CL is shown as follows.

$$\min_{\mathbf{W}, \mathbf{b}, \hat{\mathbf{W}}, \hat{\mathbf{b}}, \mathbf{P}, \mathbf{Q}, \mathbf{G}} \left\| \mathbf{X}\mathbf{W} + \mathbf{1}_n \mathbf{b}^T - \mathbf{P} \right\|_F^2 + \beta \left\| \mathbf{1}_{n \times l} - \mathbf{P} - \mathbf{Q} \right\|_F^2$$

$$+ \alpha \left\| \mathbf{X}\hat{\mathbf{W}} + \mathbf{1}_n \hat{\mathbf{b}}^T - \mathbf{Q} \right\|_F^2 + \mu \left\| \mathbf{P}^T - \mathbf{P}^T \mathbf{G} \right\|_F^2$$

$$+ \gamma \left\| \mathbf{X}^T - \mathbf{X}^T \mathbf{G} \right\|_F^2 + \lambda (\left\| \mathbf{W} \right\|_F^2 + \left\| \hat{\mathbf{W}} \right\|_F^2)$$

$$\text{s.t. } \mathbf{P} \mathbf{1}_q = \mathbf{1}_n, \mathbf{0}_{n \times l} \leq \mathbf{P} \leq \mathbf{Y}, \hat{\mathbf{Y}} \leq \mathbf{Q} \leq \mathbf{1}_{n \times l}$$

$$\mathbf{G}^T \mathbf{1}_n = \mathbf{1}_n, \mathbf{0}_{n \times n} \leq \mathbf{G} \leq \mathbf{U}$$

## EXPERIMENT

- Comparison on synthetic datasets (win/tie/loss).

	I	II	III	IV	Total
SURE	22/6/0	26/2/0	26/2/0	24/4/0	88/14/0
PL-AGGD	26/2/0	25/3/0	23/5/0	22/6/0	96/16/0
LALO	27/1/0	24/4/0	26/2/0	22/6/0	99/13/0
IPAL	28/0/0	23/5/0	26/2/0	25/3/0	102/10/0
PLDA	28/0/0	28/0/0	28/0/0	28/0/0	112/0/0
PL-KNN	28/0/0	28/0/0	28/0/0	28/0/0	112/0/0

- Comparison on real-world datasets.

Data set	FG-NET	Lost	MSRCv2	Mirflickr	Soccer Player	Yahoo!News	FG-NET(MAE3)	FG-NET(MAE5)
PL-CL	0.072 ± 0.009	0.709 ± 0.022	0.469 ± 0.016	0.642 ± 0.012	0.534 ± 0.004	0.618 ± 0.003	0.433 ± 0.022	0.575 ± 0.015
SURE	0.052 ± 0.006	0.693 ± 0.020	0.445 ± 0.021	0.631 ± 0.021	0.519 ± 0.004	0.598 ± 0.002	0.356 ± 0.015	0.494 ± 0.020
PL-AGGD	0.063 ± 0.009	0.683 ± 0.014	0.451 ± 0.012	0.610 ± 0.011	0.524 ± 0.004	0.607 ± 0.004	0.387 ± 0.015	0.530 ± 0.015
LALO	0.065 ± 0.009	0.680 ± 0.014	0.448 ± 0.015	0.626 ± 0.013	0.523 ± 0.003	0.600 ± 0.003	0.423 ± 0.020	0.566 ± 0.014
IPAL	0.051 ± 0.011	0.646 ± 0.023	0.488 ± 0.031	0.527 ± 0.009	0.528 ± 0.003	0.625 ± 0.004	0.349 ± 0.019	0.500 ± 0.019
PLDA	0.042 ± 0.005	0.289 ± 0.045	0.422 ± 0.013	0.480 ± 0.015	0.493 ± 0.003	0.380 ± 0.003	0.150 ± 0.012	0.232 ± 0.012
PL-KNN	0.036 ± 0.006	0.296 ± 0.021	0.393 ± 0.014	0.454 ± 0.015	0.483 ± 0.005	0.368 ± 0.004	0.288 ± 0.013	0.440 ± 0.016

- Comparison on transductive accuracy.

Data set	FG-NET	Lost	MSRCv2	Mirflickr	Soccer Player	Yahoo!News	FG-NET(MAE3)	FG-NET(MAE5)
PL-CL	0.159 ± 0.016	0.832 ± 0.019	0.585 ± 0.012	0.697 ± 0.016	0.715 ± 0.002	0.840 ± 0.004	0.600 ± 0.023	0.737 ± 0.018
SURE	0.158 ± 0.012	0.798 ± 0.019	0.603 ± 0.015	0.652 ± 0.022	0.700 ± 0.003	0.798 ± 0.005	0.590 ± 0.018	0.727 ± 0.019
PL-AGGD	0.130 ± 0.015	0.804 ± 0.016	0.551 ± 0.015	0.653 ± 0.015	0.698 ± 0.003	0.817 ± 0.005	0.530 ± 0.021	0.679 ± 0.024
LALO	0.153 ± 0.016	0.817 ± 0.012	0.548 ± 0.009	0.675 ± 0.017	0.698 ± 0.003	0.821 ± 0.004	0.592 ± 0.024	0.730 ± 0.015
IPAL	0.148 ± 0.021	0.793 ± 0.017	0.680 ± 0.013	0.586 ± 0.007	0.681 ± 0.003	0.839 ± 0.003	0.426 ± 0.021	0.698 ± 0.022
PLDA	0.042 ± 0.005	0.351 ± 0.060	0.479 ± 0.015	0.564 ± 0.015	0.493 ± 0.004	0.460 ± 0.009	0.150 ± 0.012	0.232 ± 0.012
PL-KNN	0.041 ± 0.007	0.338 ± 0.016	0.415 ± 0.013	0.466 ± 0.013	0.504 ± 0.005	0.403 ± 0.009	0.285 ± 0.016	0.438 ± 0.014

- Ablation study.

Kernel	Complementary Classifier	Graph	Classification Accuracy								
			FG-NET	Lost	MSRCv2	Mirflickr	Soccer Player	Yahoo!News	FG-NET(MAE3)	FG-NET(MAE5)	Average
×	×	×	0.061 ± 0.006	0.622 ± 0.019	0.381 ± 0.015	0.249 ± 0.010	0.492 ± 0.003	0.430 ± 0.051	0.402 ± 0.031	0.551 ± 0.024	0.398
✓	×	×	0.060 ± 0.008	0.654 ± 0.019	0.426 ± 0.017	0.533 ± 0.012	0.515 ± 0.010	0.526 ± 0.006	0.413 ± 0.026	0.564 ± 0.018	0.461
✓	✓	×	0.057 ± 0.009	0.705 ± 0.023	0.462 ± 0.015	0.637 ± 0.011	0.530 ± 0.004	0.517 ± 0.046	0.416 ± 0.017	0.560 ± 0.019	0.485
✓	✓	✓	0.065 ± 0.008	0.684 ± 0.022	0.456 ± 0.014	0.635 ± 0.012	0.529 ± 0.003	0.607 ± 0.003	0.426 ± 0.024	0.566 ± 0.017	0.496
✓	✓	✓	0.072 ± 0.009	0.709 ± 0.022	0.469 ± 0.016	0.642 ± 0.012	0.534 ± 0.004	0.618 ± 0.003	0.433 ± 0.022	0.575 ± 0.015	0.507
			Transductive Accuracy								
Kernel	Complementary Classifier	Graph	FG-NET	Lost	MSRCv2	Mirflickr	Soccer Player	Yahoo!News	FG-NET(MAE3)	FG-NET(MAE5)	Average
×	×	×	0.161 ± 0.017	0.729 ± 0.017	0.414 ± 0.013	0.464 ± 0.008	0.492 ± 0.004	0.439 ± 0.003	0.580 ± 0.024	0.717 ± 0.022	0.499
✓	×	×	0.159 ± 0.012	0.748 ± 0.015	0.515 ± 0.018	0.594 ± 0.013	0.700 ± 0.004	0.774 ± 0.032	0.588 ± 0.021	0.726 ± 0.010	0.600
✓	✓	×	0.141 ± 0.011	0.819 ± 0.017	0.572 ± 0.013	0.685 ± 0.014	0.714 ± 0.002	0.839 ± 0.004	0.568 ± 0.025	0.706 ± 0.022	0.630
✓	✓	×	0.150 ± 0.015	0.824 ± 0.021	0.567 ± 0.008	0.687 ± 0.012	0.701 ± 0.003	0.829 ± 0.004	0.570 ± 0.022	0.710 ± 0.021	0.629
✓	✓	✓	0.159 ± 0.016	0.832 ± 0.019	0.585 ± 0.012	0.697 ± 0.016	0.715 ± 0.002	0.840 ± 0.004	0.600 ± 0.023	0.737 ± 0.018	0.646